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Hirasugar Institute of Technology, Nidasoshi.

Inculcating Values, Promoting Prosperity

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E&C Engg. Dept.

Exam.

Internal Assessment

Odd Sem(2017-18)

SECOND INTERNAL ASSESSMENT

Sem :V

Sub: Information Theory and Coding

Sub. Code: 15EC54

Date:16/10/2017

Time:3:00pm-4:0pm

Max. Marks: 25

Note: Answer two full questions, draw sketches wherever necessary.

Q. No		Discription of Question	Marks	CO
1	a	Define source coding. Give detailed classification of source codes	4	CO304.1 CO304.2
	b	State and prove Kraft-McMillan Inequality. Test the KMI for $S_1=0$, $S_2=100$, $S_3=110$, and $S_4=111$.	8	CO304.2
OR				
2	a	What is the need for source coding? Explain the prefix property of a code with suitable examples.	4	CO304.1 CO304.2
	b	State and prove noiseless source coding theorem	8	CO304.2
3	a	Give detailed steps to devise codewords using Shanon's first encoding technique.	5	CO304.2
	b	Find the codewords for the source with $S=(A, B, C, D)$ with probabilities $P=(0.4, 0.3, 0.1, 0.2)$ using Shanons first encoding technique. Calculate coding efficiency and redundancy.	8	CO304.2
OR				
4	a	Explain the Shanon-Fano encoding algorithm.	5	CO304.2
	b	Find the codewords using Shanon-Fano algorithm for the source $S=(a, b, c, d, e, f)$ with probabilities $P=(0.15, 0.25, 0.35, 0.10)$, (Assume suitable data) $e \rightarrow 0.10, f \rightarrow 0.05$	8	CO304.2

HOD



- IA SCHEME OF EVALUATION

Sem: V		Subject: Information Theory & Coding Sub Code: 15EC54	Date: 16/10/17																
Q. No.	Bit	Description	Marks	Mapped CO's															
1	(a)	<p>Let $S \rightarrow$ be the source alphabet and $X \rightarrow$ be the code alphabet Then $S = \{s_1, s_2, \dots, s_n\}$ with $P = \{p_1, p_2, \dots, p_n\}$ & $X = \{0, 1\}$ $\Rightarrow S \rightarrow X$ mapping of each and every symbol with code alphabet combinations e.g. $s \rightarrow 0, s_1 \rightarrow 10, s_2 \rightarrow 110$ etc is called source coding.</p> <p>Classification:</p> <pre> Block codes / \ Non instantaneous / \ Instantaneous / \ Non linear / \ Linear / \ Non optimal / \ Optimal </pre>	04																
	(b)	<p>Proof of KMF</p> $\sum \frac{1}{2^{l_i}} \leq 1$ <p>for binary $\sum \frac{1}{2^{l_i}} \leq 1$</p> <p>$l_1=1, l_2=3, l_3=3, l_4=3$</p> <p>$\Rightarrow \frac{1}{2^1} + \frac{1}{2^3} + \frac{1}{2^3} + \frac{1}{2^3} = 0.875 \leq 1$ is satisfied</p>	08																
2	(a)	<p>Source coding is required for:</p> <ul style="list-style-type: none"> \rightarrow Compression of raw data \rightarrow conversion of data to digital form <p><u>Prefix Property:</u> no code word must be prefix of other</p> <p>e.g.</p> <table style="display: inline-table; vertical-align: top;"> <tr><td>s_1</td><td>0</td><td>Without prefix</td></tr> <tr><td>s_2</td><td>01</td><td>$s_1 \rightarrow 0$</td></tr> <tr><td>s_3</td><td>010</td><td>$s_2 \rightarrow 10$</td></tr> <tr><td>s_4</td><td>01011</td><td>$s_3 \rightarrow 110$</td></tr> <tr><td></td><td></td><td>$s_4 \rightarrow 1111$</td></tr> </table>	s_1	0	Without prefix	s_2	01	$s_1 \rightarrow 0$	s_3	010	$s_2 \rightarrow 10$	s_4	01011	$s_3 \rightarrow 110$			$s_4 \rightarrow 1111$	04	
s_1	0	Without prefix																	
s_2	01	$s_1 \rightarrow 0$																	
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		$s_4 \rightarrow 1111$																	

P.T.O.



- IA SCHEME OF EVALUATION

Sem: V		Subject: ITC	Sub Code: ISECS4	Date: 16/10/17	
Q. No.	Bit	Description	Marks	Mapped CO's	
2	(b)	<p>proof of source coding theorem (no. of lines)</p> <p>Let $S \rightarrow$ source symbol set -</p> <p>Then $H(S)$ be its entropy.</p> <p>\Rightarrow Lower & upper bound of $H(S)$ is governed by Shannon's source coding theorem</p> $H(S) \leq \bar{L} \leq H(S) + 1$ <p>Where \bar{L} is the average length of the code.</p>	08		
3	(a)	<p>Algorithm (Shannon's Encoding)</p> <p>\rightarrow Arrange probabilities in decreasing order</p> <p>\rightarrow find the $l_i \geq \log_2 \frac{1}{p_i}$ (to next integer)</p> <p>\rightarrow Define</p> $q_1 = 0$ $q_2 = 0 + p_1 = q_1 + p_1$ $q_3 = p_1 + p_2 = q_2 + p_2$ $q_n = p_1 + p_2 + \dots + p_n = q_{n-1} + p_n = 1.0$ <p>\Rightarrow convert q_i to q_{n-1} into binary digits bits truncated to l_i places</p> <p>\Rightarrow discard decimal points & take code only</p> <p>\Rightarrow find $H(S)$, \bar{L} & η and R</p> <p style="text-align: right;">P. 1.0</p>			



- IA SCHEME OF EVALUATION

Sem :	Subject :	Sub Code :	Date :	
V	ITC	15EC54	16/10/17	
Q. No.	Bit	Description	Marks	Mapped CO's
3	(b)	<p>A 0.4 $\Rightarrow l_1 \geq \log \frac{1}{p_A} \Rightarrow 2$ B 0.3 $\Rightarrow l_2 \geq \log \frac{1}{p_B} \Rightarrow 2$ D 0.2 $\Rightarrow l_3 \geq \log \frac{1}{p_D} \Rightarrow 3$ E 0.1 $\Rightarrow l_4 \geq \log \frac{1}{p_E} \Rightarrow 4$</p> <p> $q_1 = 0 \rightarrow 0.00$ $q_2 = 0.4 \rightarrow 0.01$ $q_3 = 0.7 \rightarrow 0.101$ $q_4 = 0.9 \rightarrow 0.1110$ $q_5 = 1.0$ </p> <p> $\Rightarrow A \rightarrow 00 \quad B \rightarrow 10 \quad D \rightarrow 101 \quad E \rightarrow 1110$ </p> <p> $Z = 2 \times 0.4 + 2 \times 0.3 + 3 \times 0.2 + 4 \times 0.1$ $= 0.8 + 0.6 + 0.6 + 0.4 = 2.4$ </p> <p> $H(S) = 1.825$ $\therefore \eta = \frac{1.825}{2.4} = 0.7604 \approx 76.04\%$ $R = 1 - \eta = 23.12\%$ </p>		



- IA SCHEME OF EVALUATION

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Sem: V Subject: ITC Sub Code: 15EC54 Date: 16/10/17																												
4	(a)	<p>Algorithm (Shanon-fano)</p> <ul style="list-style-type: none"> → Arrange probabilities in decreasing order → Divide into two groups such that probabilities are more or less equal → Assign bit 0 to upper group & 1 to lower group → repeat above steps till no further division is possible → Readout the codes 																										
	(b)	<p>assuming</p> <table style="margin-left: 20px;"> <tr> <td>c</td> <td>→ 0.35</td> <td>0</td> <td>0</td> </tr> <tr> <td>b</td> <td>→ 0.25</td> <td>0</td> <td>1</td> </tr> <tr> <td>a</td> <td>→ 0.15</td> <td>1</td> <td>0</td> </tr> <tr> <td>d</td> <td>→ 0.10</td> <td>1</td> <td>0</td> </tr> <tr> <td>e</td> <td>→ 0.05</td> <td>1</td> <td>1</td> </tr> <tr> <td>f</td> <td>→ 0.05</td> <td>1</td> <td>1</td> </tr> </table> <p style="margin-left: 20px;"> $P(e) = 0.10$ $P(f) = 0.05$ </p> <p style="margin-left: 20px;"> c → 00 b → 01 a → 100 d → 101 e → 110 f → 111 </p>	c	→ 0.35	0	0	b	→ 0.25	0	1	a	→ 0.15	1	0	d	→ 0.10	1	0	e	→ 0.05	1	1	f	→ 0.05	1	1		
c	→ 0.35	0	0																									
b	→ 0.25	0	1																									
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